

Layout of Presentation

- What is S(W)AXS?
 - How do we do S(W)AXS?

Applications:

- Solution Scattering
- Model membranes
- Grazing Incidence Studies
- Hierarchical Materials

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SAXS and WAXS



X-rays



Andre Guinier

The pioneers of Small Angle Scattering

Otto Kratky

DETECTOR

Beam Stop

SAXS

WAXS

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SAXS and WAXS



Small – Angle : Supramolecular Envelope

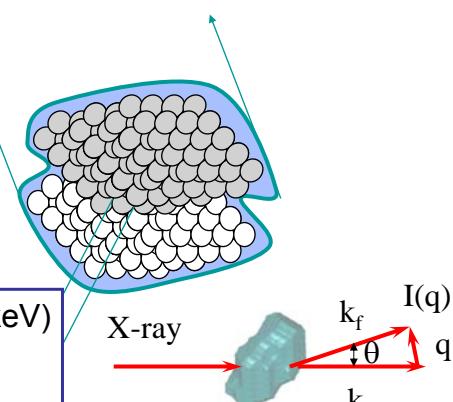
Bragg's law:

$$\sin \theta/2 = \lambda / 2d$$

small θ large d

For CuK α 0.154 nm (8 keV)

20 deg	0.5 nm
0.9 deg	10 nm
0.09 deg	100 nm

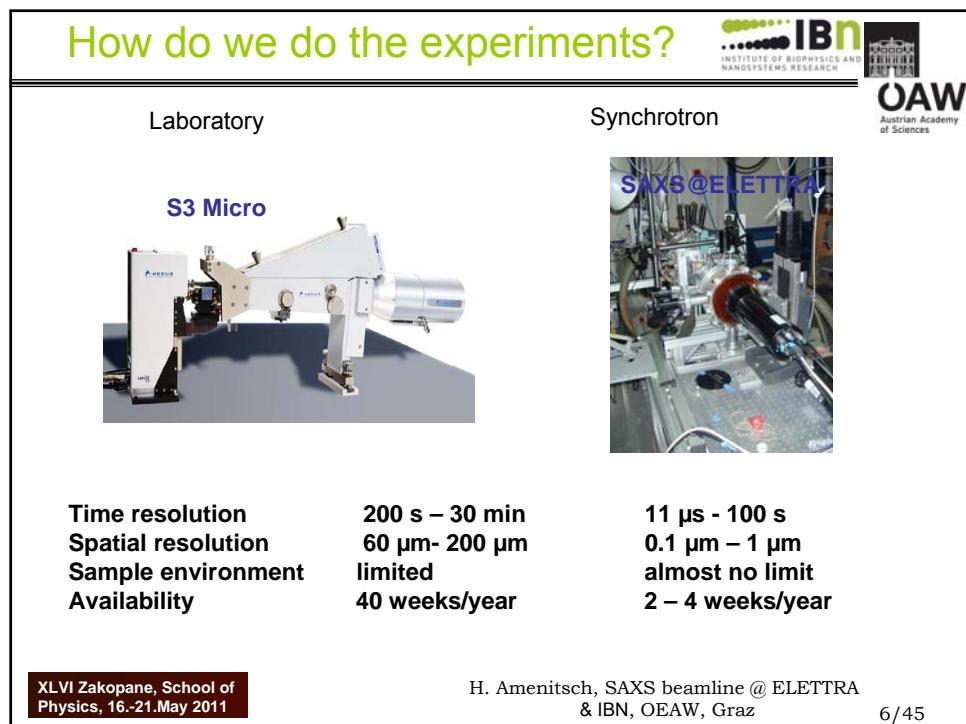
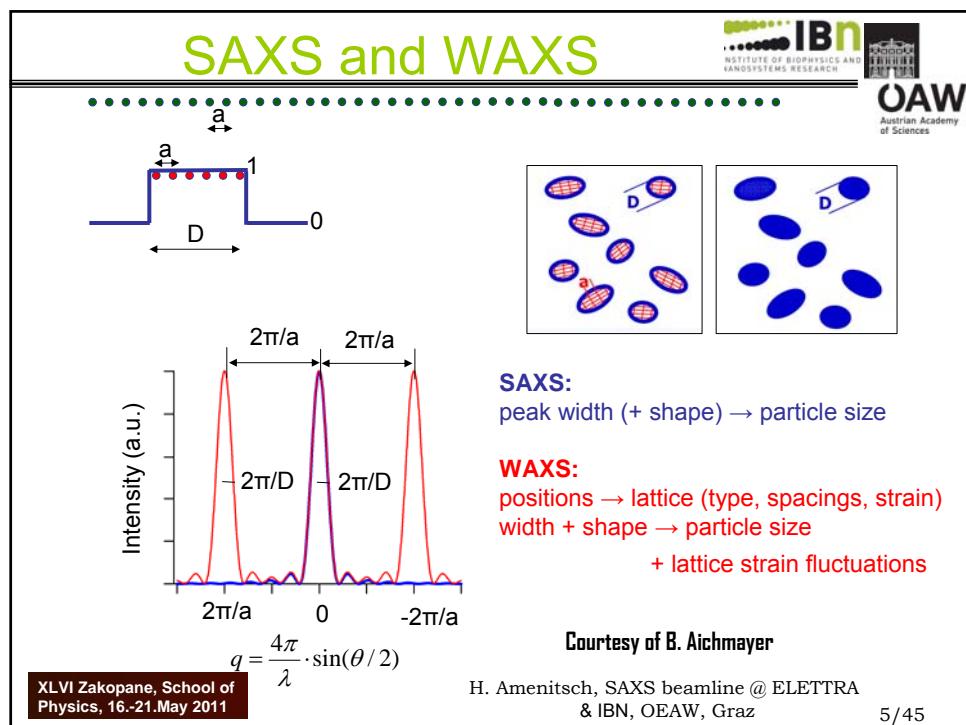


Molecular Lattice

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Sample Environment

IBN
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NANOSYSTEMS RESEARCH

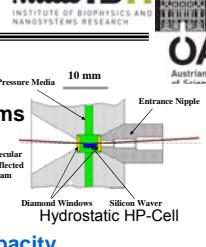
OAW
Austrian Academy
of Sciences

Temperature
 $-195^{\circ}\text{C} - 300^{\circ}\text{C}$
 $20^{\circ}\text{C} / 2\text{ ms}$



Peltier Moduls / Oxford Cryostream

Pressure
 $0 - 3 \text{ Kbar}$
 $3000 \text{ bar} / 10 \text{ ms}$



Pressure Media 10 mm
 Specular reflected beam
 Diamond Windows
 Hydrostatic HP-Cell
 Entrance Nipple
 Silicon Wave Cell

Chemical Potential
 $50 \text{ ms} / 70 \mu\text{s}$



Biologic SFM-4

μ

A

B

X-ray beam

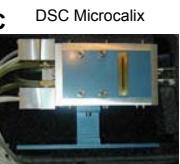
jet

time

q

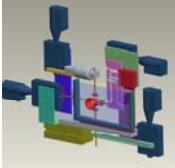
$\mu\text{Fluidics}$

Heat capacity
 $10^{\circ}\text{C} - 150^{\circ}\text{C}$
 $^{\circ}\text{C}/\text{min}$



DSC Microcalix

μ Parameters
 tension



Biaxial Device

11th Annual Report

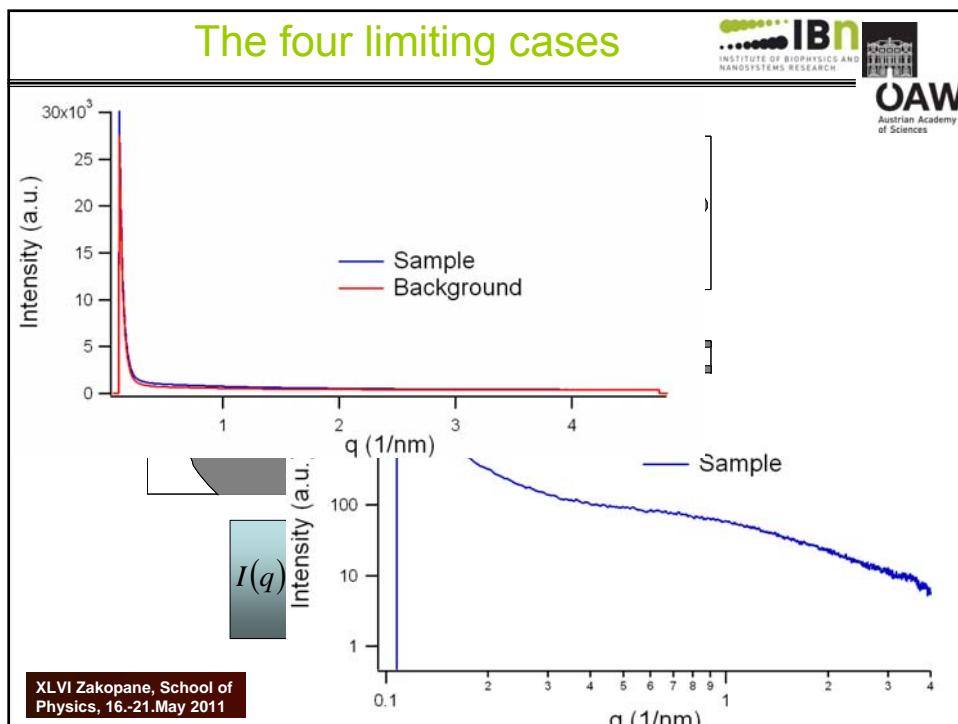
AUSTRIAN BIOPHYSICS AT

User: IR-Spectroscopy, UV-vis, Ellipsometer

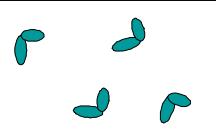
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Dilute Monodisperse Systems



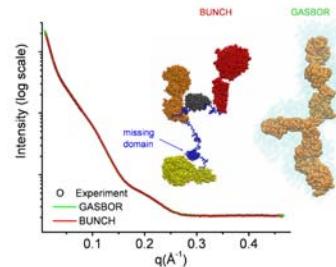
Parameters

- Radius of Gyration
- Particle weight
- Particle Volume

Examples:

- Protein solutions
- Polymer solutions
- Nanoparticles

Particle Shape

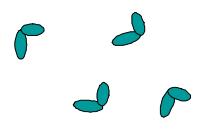


GASBOR, DAMMIN(F), Svergun D.I. et al.

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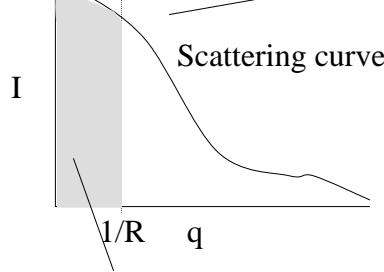
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Guinier's Law



Radius of Gyration

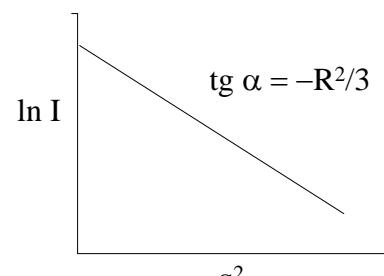
$$I(q) = I(0) \cdot e^{-R^2 q^2 / 3}$$



Guinier Range:

Limited to $q < 1/R$!

Guinier Plot



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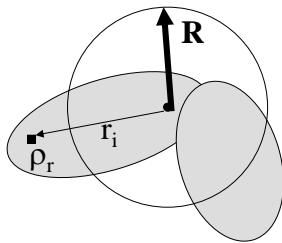
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Guinier's Law



Radius of Gyration



$$R^2 = \frac{\int r^2 (\Delta\rho_r) d^3r}{\int \Delta\rho_r d^3r}$$

Ellipsoid with semiaxes a,b,c:

$$R = \sqrt{\frac{a^2 + b^2 + c^2}{5}}$$

Sphere with radius r:

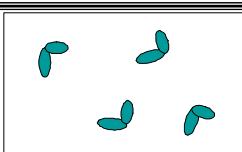
$$R = \sqrt{\frac{3}{5}} \cdot r = 0.77 \cdot r$$

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Real Space Function

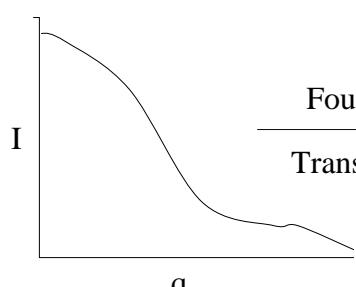


$$I(q) = |A(q)|^2 = V \cdot \int p(r) \cdot e^{-iqr} d^3r$$

Scattering Space Function

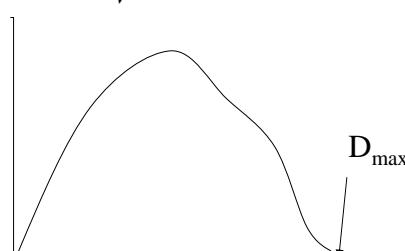
Real Space Function

$$p(r) = \frac{1}{V} \int \rho(r_0) \rho(r_0 + r) dr_0$$



Scattering curve

Fourier
Transform



Electron Pair Distance

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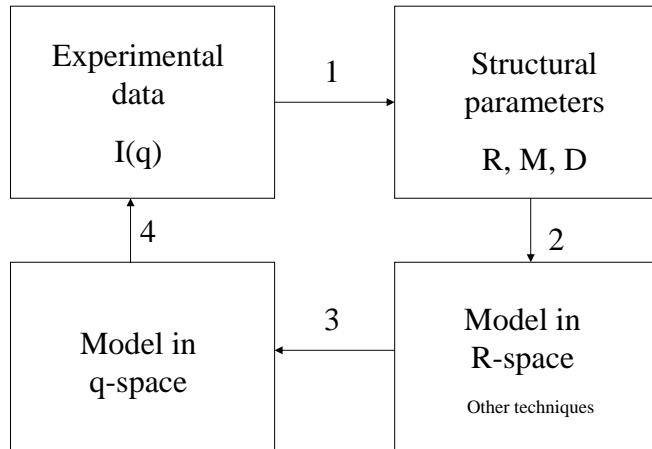
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How Do You Obtain Information?



General strategy for solving
structural problems with SAXS



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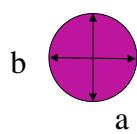
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Globular and Non-Globular Particals



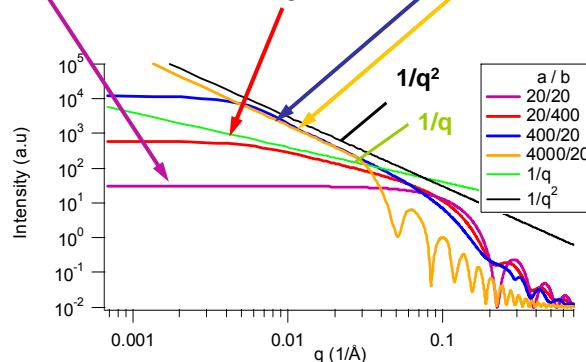
3D Case $a=b$



2D Case $b \gg a$



1D Case $b \ll a$



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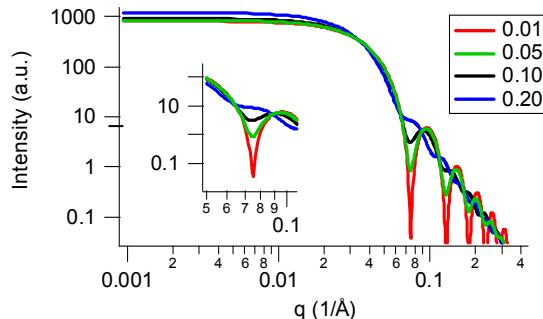
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Size Distributions



$$I(q) = \int D_n(R) \cdot R^n \cdot i_o(qR) \cdot dq$$

$i_0(x)$ Formfactor
 $n=6: D_6$ number distribution
 $n=3: D_3$ volume distribution
 $n=0: D_0$ intensity distribution



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Scattered Intensity



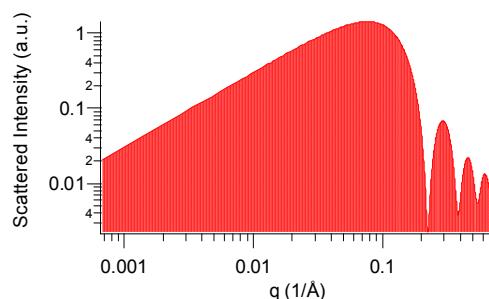
Scatter Probability

$$\Sigma \cdot D_s \propto \int I(q) \cdot q \cdot dq \propto p \cdot \Delta\rho^2 \cdot l_c$$

Makroscopic Cross Section
 D_s Sample Thickness

p Volume Fraction
 $\Delta\rho$ Electron Density Contrast
 l_c Correlation Length
R Radius

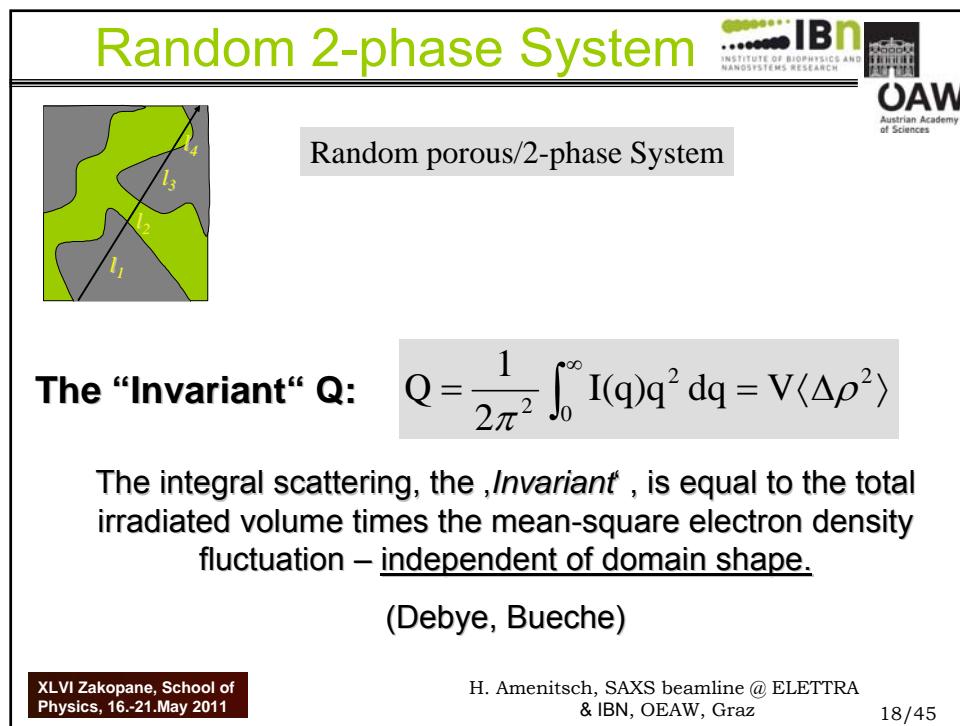
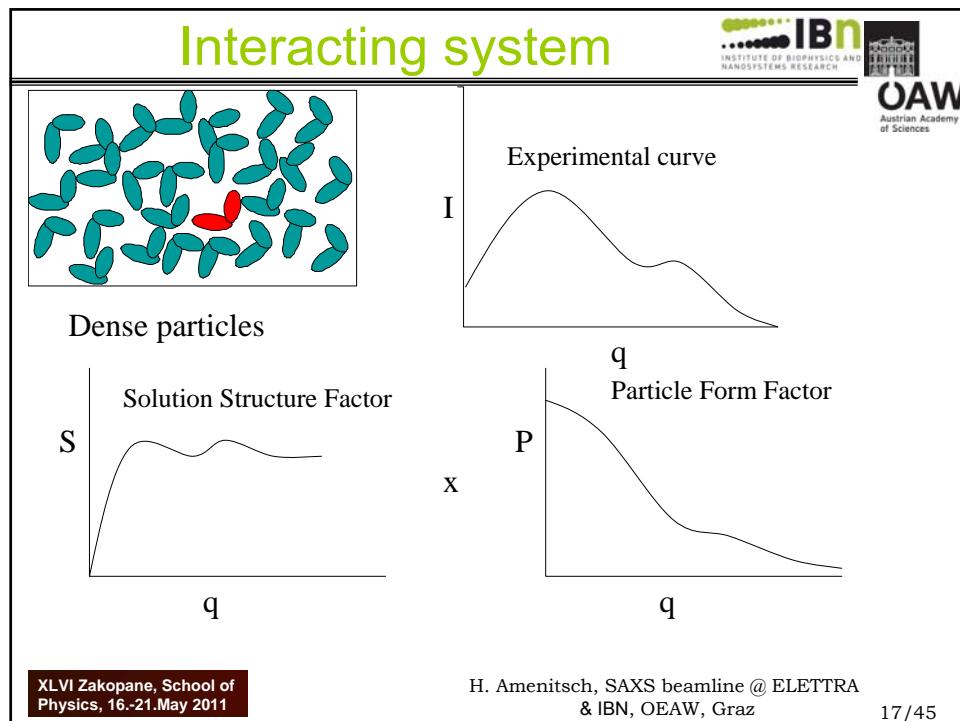
Sphere: 20 Å, $l_c = 3/2 R$



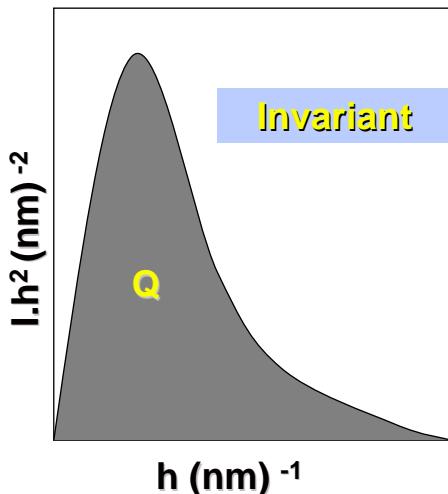
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Invariant



Q has the dimension of a reciprocal volume

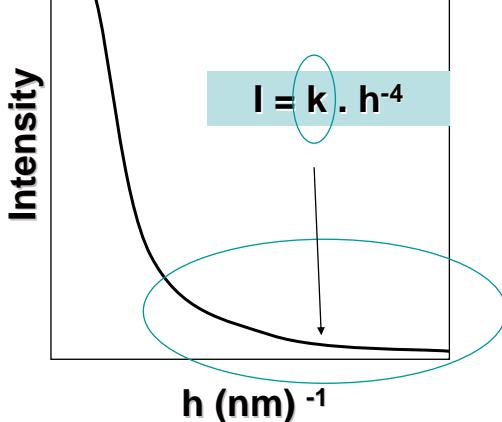
Invariant

In the case of a two-phase system (e.g. crystalline/ amorphous polymer), the invariant is related to the volume fractions ϕ , and the electron densities ρ_c and ρ_a

$$Q = V(\rho_c - \rho_a)^2 \cdot \phi_a \phi_c$$

**total irradiated
volume**

Porod's Law



Towards larger angles, the intensity decays with the fourth power of the angle (Porod's law)

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Porod's Law



The decay constant k from a two-phase system is given by

$$k = \lim_{h \rightarrow \infty} h^4 \cdot I(h) = 2\pi \cdot S \cdot (\rho_c - \rho_a)^2$$

K depends on the total inner surface and the mean-square electron density fluctuations

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How Do You Use It?



Combining *Invariant Q* and *Tail-End Constant k*, obtained from one single measurement

$$\frac{k}{Q} = \frac{2\pi \cdot S_i}{\phi(1-\phi)}$$

if ϕ is around 0.5, the value of S_i is not very sensitive to variations in ϕ .

Combining Scattered Intensity and *Invariant Q*

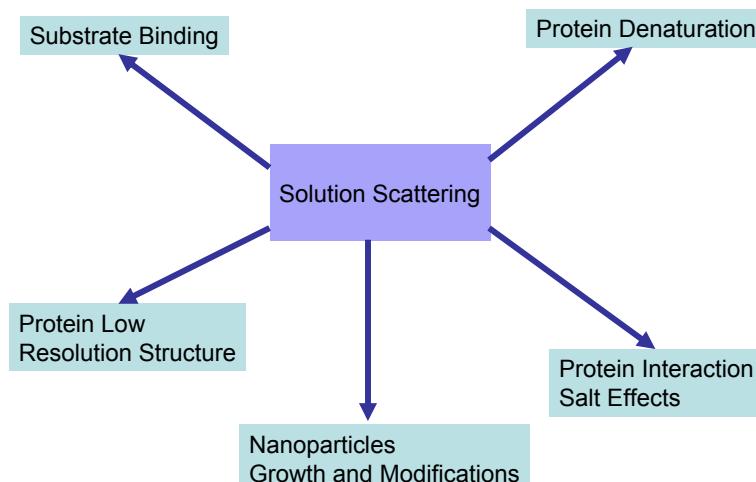
$$\frac{\Sigma \cdot D_s}{Q} = \frac{\int dq \cdot q \cdot I(q)}{\int dq \cdot q^2 \cdot I(q)} = \frac{1}{2 \cdot \pi} \cdot l_c$$

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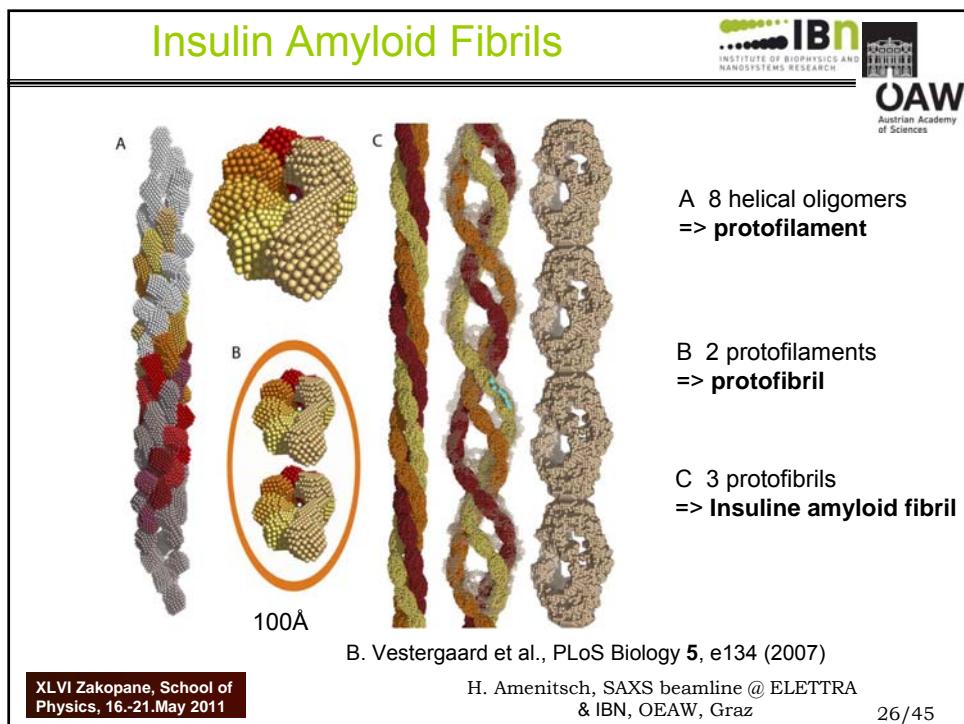
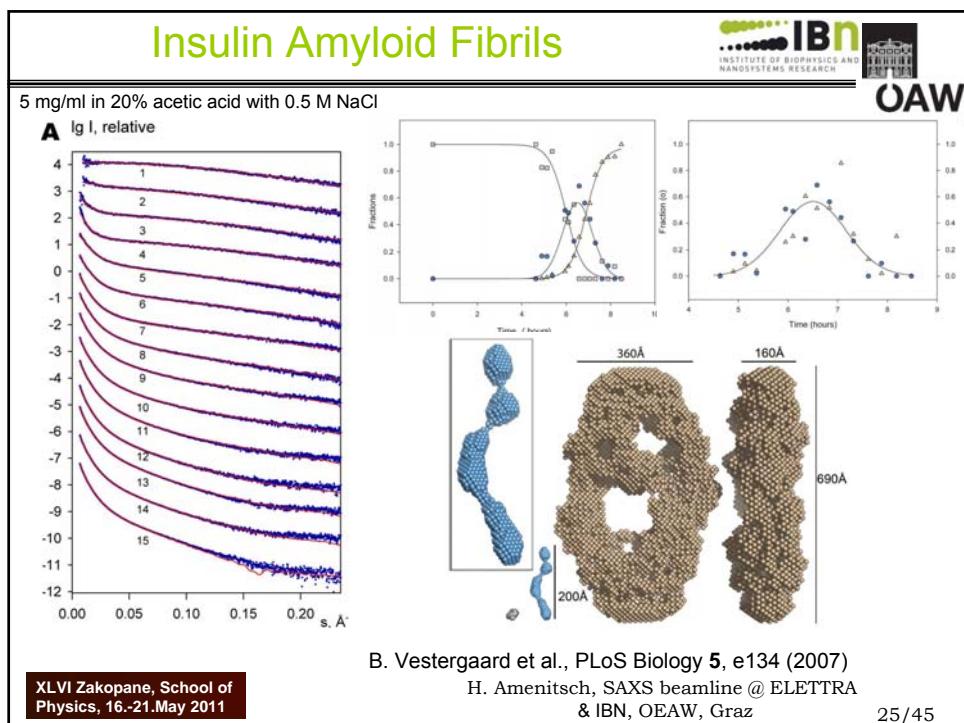
Solution Scattering

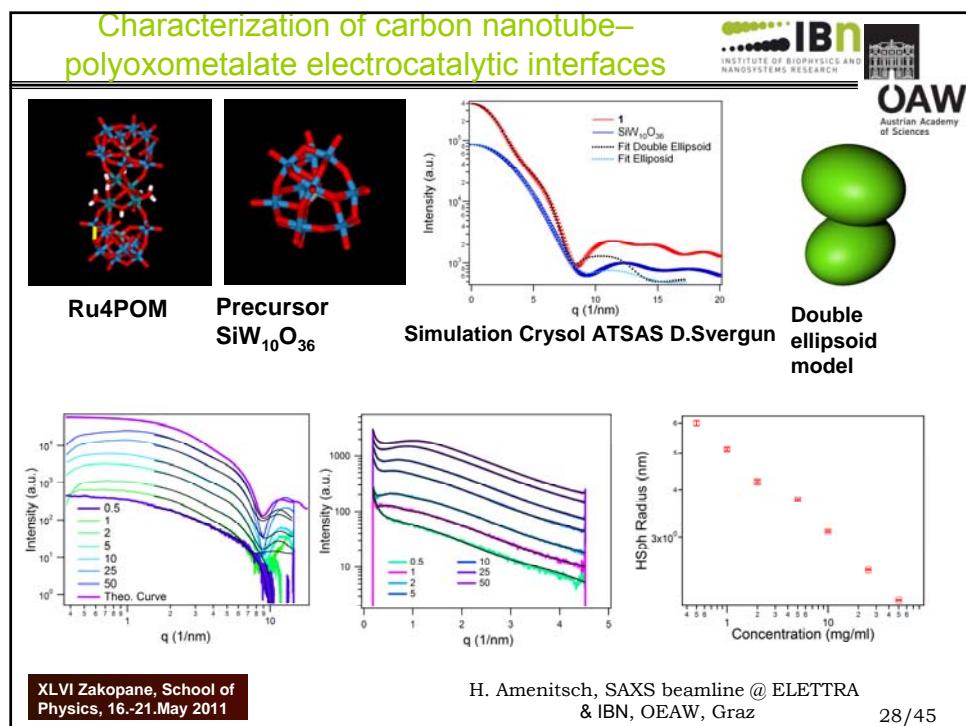
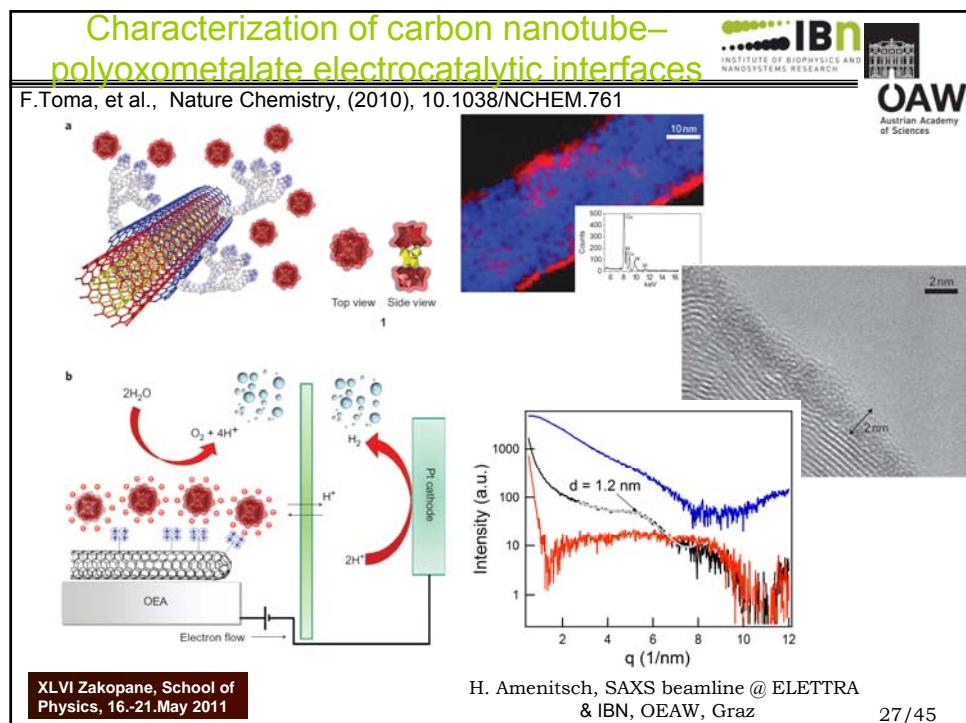


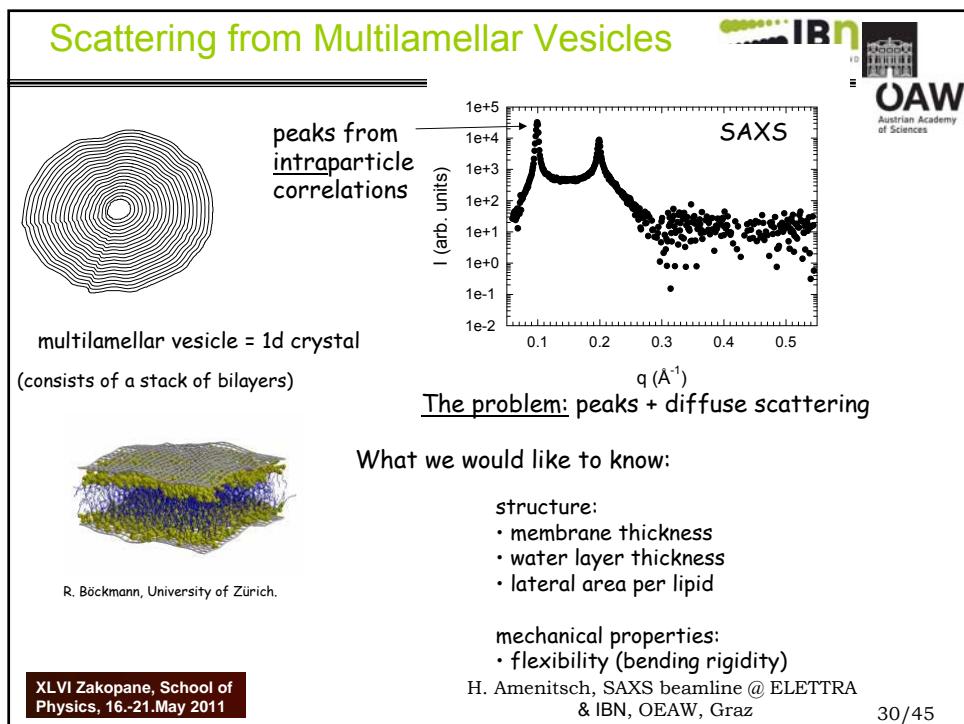
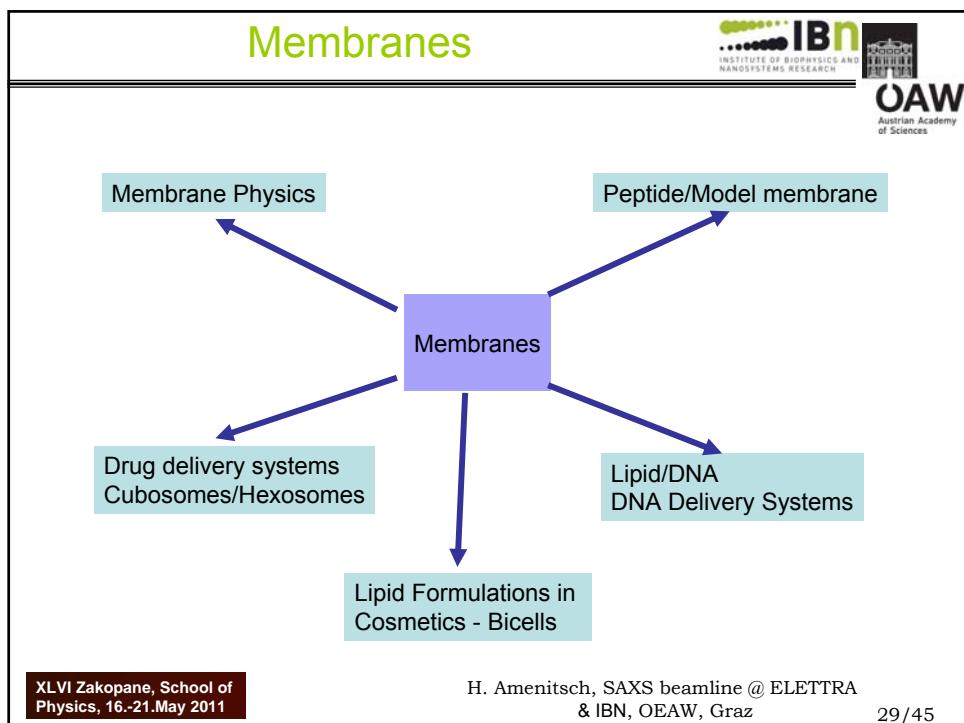
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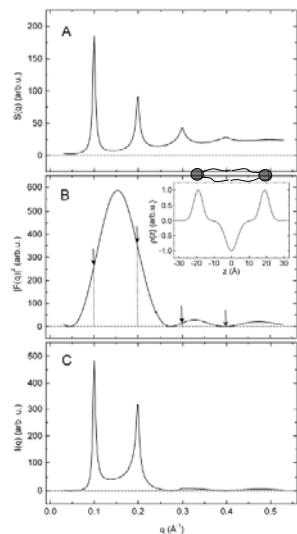




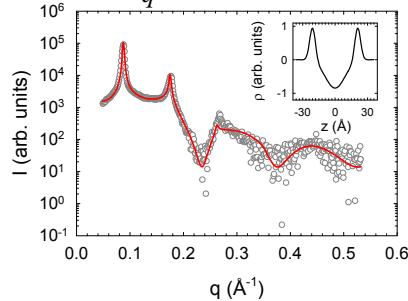
The Global Model



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$$I(q) = \frac{S(q)|F(q)|^2}{q^2}$$



structure:

- membrane thickness
- water layer thickness
- lateral area per lipid
- mechanical properties:
- flexibility (bending rigidity)

G. Pabst, M. Rappolt, H. Amenitsch, P. Laggner, Phys. Rev. E **62**, 4000 (2000).

H. Amenitsch, SAXS beamline @ ELETTRA

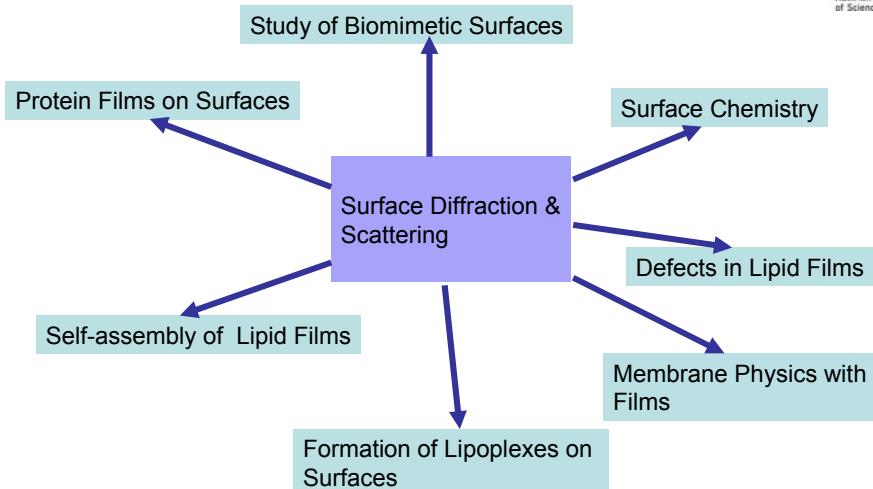
& IBN, OEW, Graz

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Surface Diffraction & Scattering



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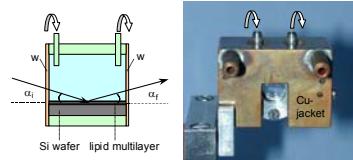


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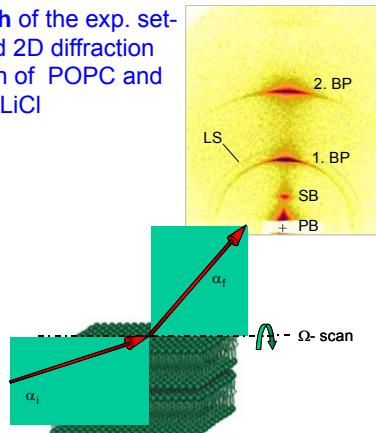
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Surface Chemistry



Sketch of the exp. set-up and 2D diffraction pattern of POPC and 0.5 M LiCl



Sketch and photograph of the sample cell in transmission geometry for GISAXS.

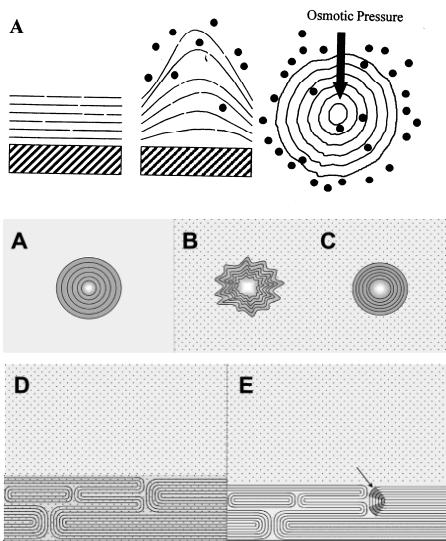
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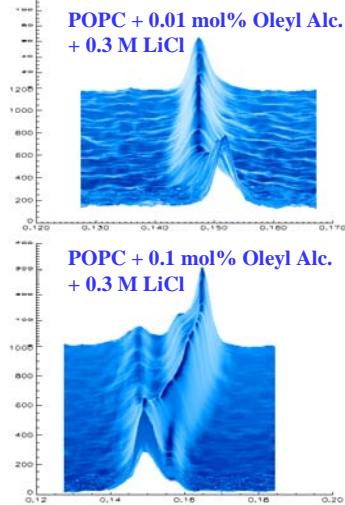
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Surface Chemistry



POPC + 0.01 mol% Oleyl Alc.
+ 0.3 M LiCl



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Amenisch, H., et al., (2004) Langmuir

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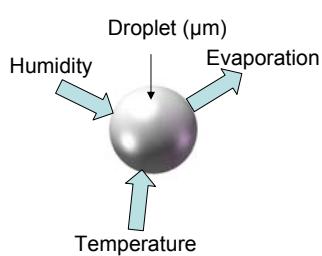
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In situ aerosol synthesis



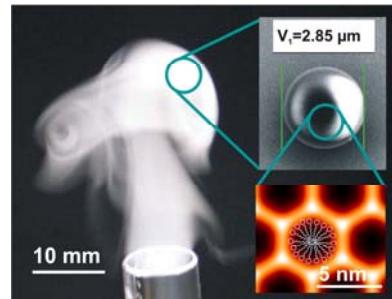
Scientific case

Aerosol-Microreactor



Mesostructured Si produced by Evaporation Induced Self Assembly (EISA)*

*Y. F. Lu et al., *Nature* 398, 223-226 (1999).



CTAB:TEOS:H₂O:HCl
molar ratio - 0.14:1:41:0.13

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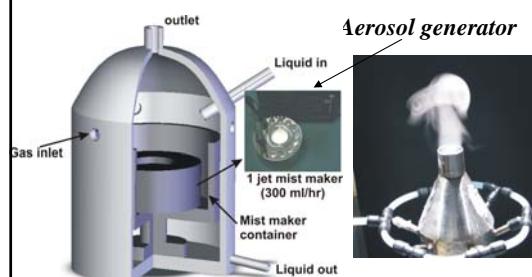
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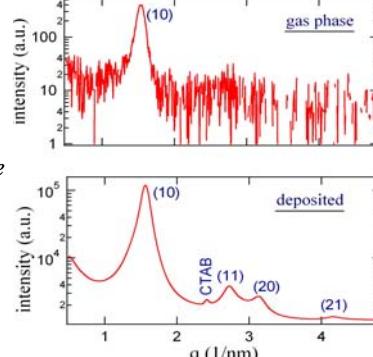
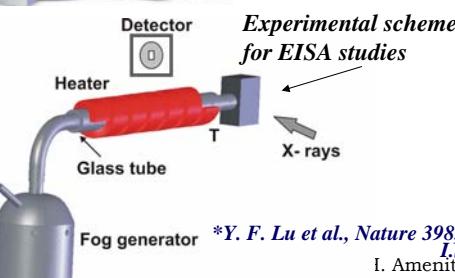
Gas phase study of Silica Self Assembly



Mesostructured Si produced by Evaporation Induced Self Assembly (EISA)*



CTAB:TEOS:H₂O:HCl
molar ratio - 0.14:1:41:0.13



*Y. F. Lu et al., *Nature* 398, 223-226 (1999).

I. Shyjumon et al., *Rev. Sci. Ins.* 79, 43905 (2008)

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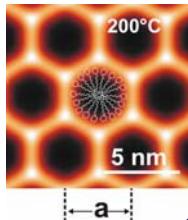
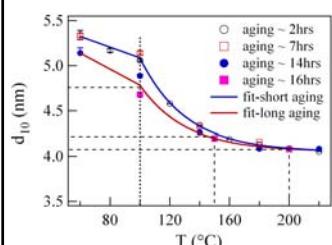
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Electron density map & model fitting

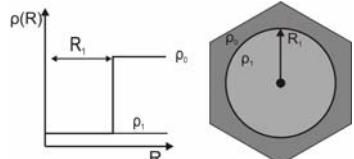


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electron density maps of (- + +) phase from (10), (11), (20) & (21) integrated intensities

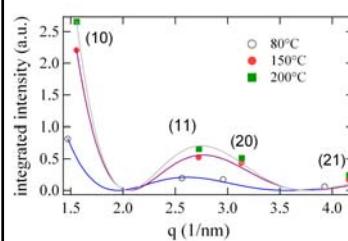


The two density regime model



$$I(q) = k \left[\frac{2J_1(qR_1)}{(qR_1)} \right]^2$$

model fit using the two density regime model



R₁ - radius of the core, a - cell parameter
& Silica matrix thickness = (a - 2R₁)

T (°C)	R ₁ (nm)	a (nm)	Silica matrix(nm)
80	1.964±0.041	4.933±0.001	1.005 ±0.043
150	1.857±0.035	4.666±0.001	0.9516±0.037
200	1.868±0.037	4.664±0.001	0.9282±0.039

I.Shyjumon et al., Langmuir, 2011

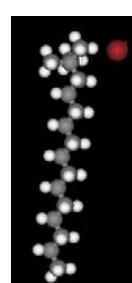
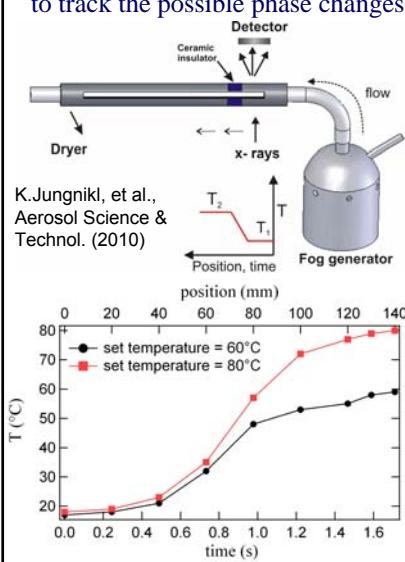
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In situ analysis of Si mesophase formation

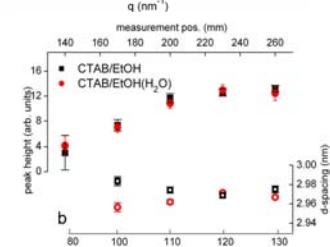
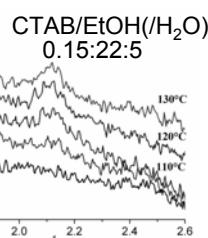


- Temperature profile inside the dryer is adjusted to track the possible phase changes of silica

- Test of Set-up Crystallization of CTAB

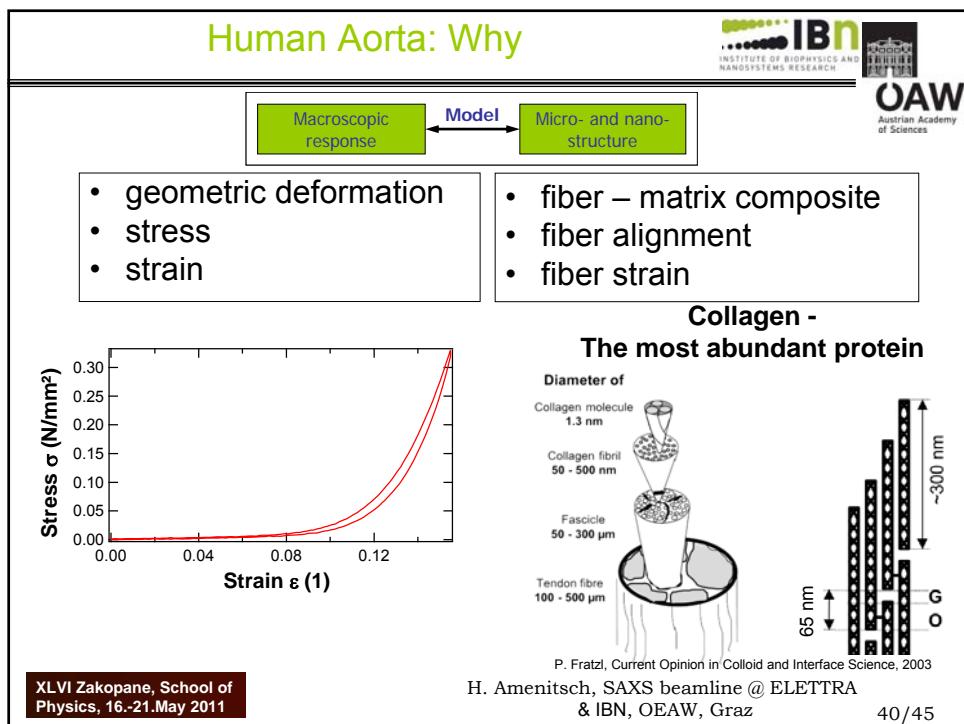
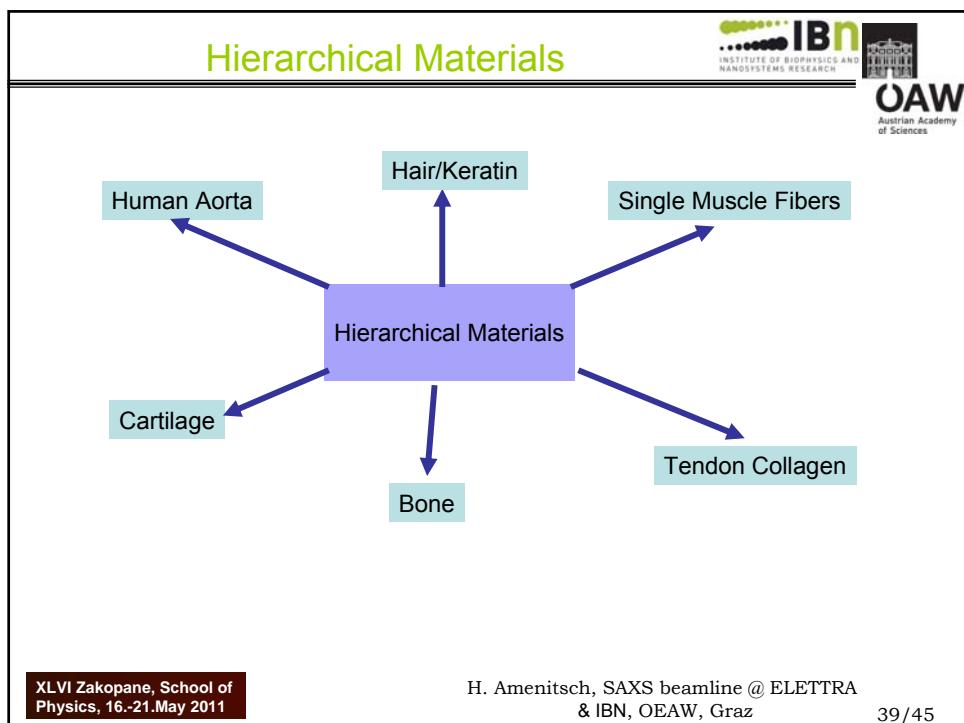


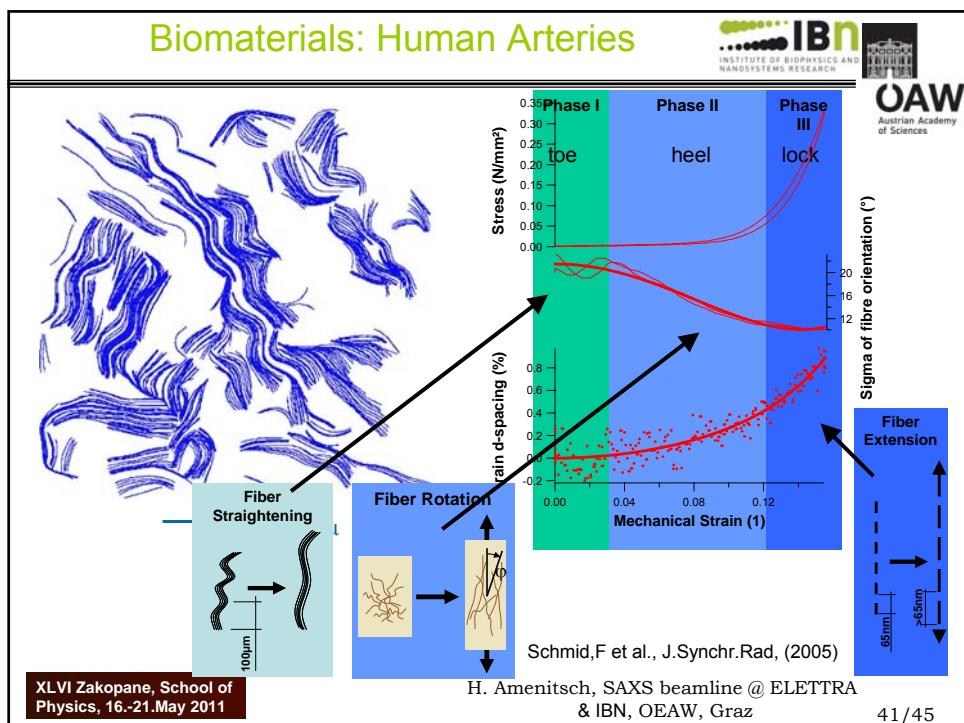
K.Jungniki, et al.,
Aerosol Science &
Technol. (2010)



H. Amenitsch,
& IBN, OEAW, Graz

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Conclusion & Outlook



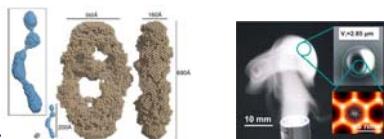
Conclusion

SAXS:

- What is S(W)AXS?
- How do we do S(W)AXS?

Applications:

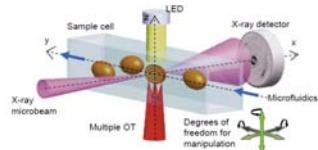
- Solution Scattering
- Model membranes
- Grazing Incidence Studies
- Hierarchical Materials



Outlook μFluidics



Optical Tweezer



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Acknowledgement



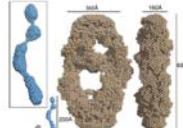
B.Vestergaard, D.Svergun,
Univ. Kopenhagen/EMBL

F.Toma, M.Prato, G.Scolles,
Univ. Trieste, ELETTRA, SISSA

G.Pabst, K.Lohner, IBN, Graz
Yagmur, A, Univ. Copenhagen

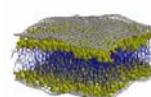
D.Grosso, C.Sanchez, Univ. Paris

G. Holzapfel, TU-Graz, Stockholm



Insulin

Membranes



Human Arteries



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